

```

> restart;
with(plots):
with(StringTools):
with(LinearAlgebra):
with(DEtools):

#####

Region:='Mosobl'; url:="https://gogov.ru/covid-19/mo#data";

#valp := [12.0545284599666, 40487.7036090492, 0.0878540675828671, 0.119034763474605,
0.208571881538399, 0.163876229453231, #0.0804863589181470, 0.0940935501988715, 0.105057419991328,
0.104244846871936, 0.00441107479765352, 0.00987259141378349, #0.0000931839501779284];

valp:=readdata(cat(Region,`3c.txt`));

#####

fdisplay:=proc(f,p)
  print(cat(f,`.jpg`)); #print(cat(f,`.eps`));
  plotsetup(jpeg,plotoutput=cat(f,`.jpg`),plotoptions=`noborder`); print(display(p));
  plotsetup(ps,plotoutput=cat(f,`.eps`),plotoptions=`noborder`); print(display(p));
  plotsetup(default,plotoptions=`noborder`): print(display(p));
end:

pr:=proc(x) print(x); x; end:

grad:=(F,V)->map(q->diff(F,q),V):

linsplit:=(F,V)->subs(map(q->q=0,V),[op(grad(F,V)),F]):

corr:=proc(x,y) local i; seq(x[i]=y[i],i=1..nops(x)): end:

ssum:=(F,V)->convert([seq(F,V)],`+`):

pprod:=(F,V)->convert([seq(F,V)],`*`):

Lag:=proc(t,tx,kx) local i,j;
  ssum(kx[i]*pprod(piecewise(j=i,1,(t-tx[j])/(tx[i]-tx[j])),j=1..nops(tx)),i=1..nops(tx)):
end:

```

```
Lag(t, [ta, tb], [a, b]); Lag(t, [ta, tb, tc], [a, b, c]);
```

```
pi:=evalf(Pi);
```

```
gM:=evalf(solve((1-x)^2=x,x)[2]):
```

```
goldMin:=proc(f,T,epsilon) local a,b,c,d,fa,fb,fc,fd,k;
```

```
  a:=op(1,T); b:=op(2,T); fa:=f(a); fb:=f(b); k:=0;
```

```
  c:=a+(b-a)*gM; fc:=f(c); d:=b-(b-a)*gM; fd:=f(d);
```

```
  while abs(a-b)>epsilon do: k:=k+1;
```

```
    if fc>fd then a:=c; fa:=fc; c:=d; fc:=fd; d:=b-(b-a)*gM; fd:=f(d);
```

```
    else b:=d; fb:=fd; d:=c; fd:=fc; c:=a+(b-a)*gM; fc:=f(c);
```

```
    fi;
```

```
  od: #print(k);
```

```
  (a+b)/2;
```

```
end:
```

```
findMin1:=proc(F,V) local f,df,f0,f1,f2,V0,V1,V2,ff,t,dt,i,j;
```

```
  ff:=V->F(op(evalf(map(exp,V)))); V1:=evalf(map(ln,V)); f1:=F(op(V));
```

```
  f:=[seq(F(seq(evalf(exp(V1[j]+piecewise(j=i,0.0001,0))),j=1..nops(V))),i=1..nops(V))];
```

```
  df:=[seq((f[j]-f1)/0.1,j=1..nops(V))];
```

```
  V0:=V1-0.001*df; f0:=ff(V0); V2:=V1+0.001*df; f2:=ff(V2);
```

```
  dt:=0.0001; while f0<f1 do: V2:=V1; f2:=f1; V1:=V0; f1:=f0; V0:=V0-dt*df; f0:=ff(V0); dt:=dt*1.1; od;
```

```
  dt:=0.0001; while f2<f1 do: V0:=V1; f0:=f1; V1:=V2; f1:=f2; V2:=V2+dt*df; f2:=ff(V2); dt:=dt*1.1; od;
```

```
  t:=goldMin(t->ff(t*V0+(1-t)*V2),0..1,0.0001);
```

```
  map(exp,t*V0+(1-t)*V2);
```

```
end:
```

```
findMin:=proc(F,V) local V1,Z1,Z2;
```

```
  Z2:=pr(F(op(V))); V1:=findMin1(F,V); Z1:=pr(chi2(op(V1)));
```

```
  while abs(1-Z1/Z2)>0.0001 do: Z2:=Z1; V1:=findMin1(F,V1); Z1:=pr(chi2(op(V1))); end;
```

```
  V1;
```

```
end:
```

Region := Mosobl

url := "https://gogov.ru/covid-19/mo#data"

valp := [12.11547222, 40685.61891, 0.08860157496, 0.1194914102, 0.206504248, 0.1639018944, 0.08136304104, 0.09362917651,

0.1050655024, 0.104521194, 0.004380244938, 0.01024923215, 0.00009329616206]

$$\frac{a(t-tb)}{ta-tb} + \frac{b(t-ta)}{tb-ta}$$

$$\frac{a(t-tb)(t-tc)}{(ta-tb)(ta-tc)} + \frac{b(t-ta)(t-tc)}{(tb-ta)(tb-tc)} + \frac{c(t-ta)(t-tb)}{(tc-ta)(tc-tb)}$$

$$\pi := 3.141592654$$

(1)

```
> =====`;  
`VERHULST FITTING`;  
`=====`;
```

=====

VERHULST FITTING

=====

(2)

```
> f_:=d->sum(a[j]*d^j,j=0..n); fe_:=d->sum(a[j]*d^j,j=0..ne);  
  
M:='M':  
ff:=x->M*(1-1/(exp(x)+1)); ff_:=unapply(solve(y=ff(x),x),y); diff(ff_(x),x); dff_:=unapply  
(simplify(%,x),x);  
ffe:=x->exp(x); ffe_:=unapply(solve(y=ffe(x),x),y); diff(ff_(x),x); dffe_:=unapply(simplify(%,  
x),x);  
  
sigma:=x->simplify(sqrt(x));  
  
chi2:=(T,f_)->simplify(sum(evalf(ff_(T[k])-f_(k))^2/dff_(T[k])^2/sigma(T[k])^2,k=1..nops(T)));  
chi2e:=(T,f_)->simplify(sum(evalf(ff_(T[k])-f_(k))^2/dffe_(T[k])^2/sigma(T[k])^2,k=1..nops(T)));  
  
F:=proc(T,chi2,f_) chi2(T,f_);  
  indets(%); grad(%%,%); subs(solve(%,%%),f_(i)); unapply(%,i);  
end;
```

$$f_ := d \mapsto \sum_{j=0}^n a_j \cdot d^j$$

$$fe_ := d \mapsto \sum_{j=0}^{ne} a_j \cdot d^j$$

$$ff := x \mapsto M \cdot \left(1 - \frac{1}{e^x + 1} \right)$$

$$ff_ := y \mapsto \ln \left(\frac{y}{M-y} \right)$$

$$\frac{\left(\frac{1}{M-x} + \frac{x}{(M-x)^2} \right) (M-x)}{x}$$

$$dff_ := x \mapsto \frac{M}{(M-x) \cdot x}$$

$$ffe := x \mapsto e^x$$

$$ffe_ := y \mapsto \ln(y)$$

$$\frac{1}{x}$$

$$dffe_ := x \mapsto \frac{1}{x}$$

$$\sigma := x \mapsto \text{simplify}(\sqrt{x})$$

$$\chi_2 := (T, f_) \rightarrow \text{simplify} \left(\sum_{k=1}^{nops(T)} \frac{\text{evalf}(ff_ (T_k) - f_ (k))^2}{dff_ (T_k)^2 \sigma(T_k)^2} \right)$$

$$\chi_{2e} := (T, f_) \rightarrow \text{simplify} \left(\sum_{k=1}^{nops(T)} \frac{\text{evalf}(ffe_ (T_k) - f_ (k))^2}{dffe_ (T_k)^2 \sigma(T_k)^2} \right)$$

(3)

```
> dig:={"0","1","2","3","4","5","6","7","8","9","0"}: val:=proc() global data,i; local j,f; f:=0;
  while not(data[i] in dig) or f=1 and data[i] in {"+"} union dig do:
    if f=1 and not(data[i] in dig) then f:=0; else if data[i]="+" then f:=1; fi fi; i:=i+1: od:
    j:=i; while (data[i] in dig or data[i] in {"-","+"}) do i:=i+1: od: parse(data[j..i-1]);
  end:
  ``; Region; status,data,headers:=HTTP:-Get(url): HTTP:-Code(status); i:=Search("<th>",data):

iter:=proc() global i; local r;
  r:=val(); if data[i]<>"." then NULL else [r,val(),val(),val(),val(),val()],iter() fi;
```

end:

```
[iter()]: tA:=[seq(%[nops(%) +1-i],i=1..nops(%))];  
dd:=tA[1][1]+piecewise(tA[1][2]=2,-29,tA[1][2]=4,31,0)-1;  
T:=map(q->q[4],tA): #writedata(Region || `-i.txt`,%): #  
T3:=map(q->q[5],tA): #writedata(Region || `-m.txt`,%): #  
T1:=map(q->q[6],tA): #writedata(Region || `-r.txt`,%): #  
T2:=[seq(T[i]-(T1[i]+T3[i]),i=1..nops(T))]: #writedata(Region || `-h.txt`,%): #  
i:='i':  
Region; 'T'=T; 'T1'=T1; 'T2'=T2; 'T3'=T3;  
  
nops(T); [i+dd $ i=1..%];
```

``
Mosobl
"OK"

```
tA := [[8, 3, 20, 1, 0, 0], [9, 3, 20, 1, 0, 0], [10, 3, 20, 1, 0, 0], [11, 3, 20, 3, 0, 0], [12, 3, 20, 3, 0, 0], [13, 3, 20, 4, 0, 0], [14, 3, 20, 5, 0, 0],  
[15, 3, 20, 8, 0, 0], [16, 3, 20, 9, 0, 0], [17, 3, 20, 11, 0, 0], [18, 3, 20, 12, 0, 0], [19, 3, 20, 17, 0, 0], [20, 3, 20, 18, 0, 1], [21, 3, 20, 35,  
0, 1], [22, 3, 20, 35, 0, 1], [23, 3, 20, 35, 0, 1], [24, 3, 20, 35, 0, 2], [25, 3, 20, 41, 0, 7], [26, 3, 20, 41, 0, 7], [27, 3, 20, 49, 0, 8], [28, 3,  
20, 85, 0, 8], [29, 3, 20, 112, 0, 10], [30, 3, 20, 119, 0, 10], [31, 3, 20, 119, 0, 14], [1, 4, 20, 134, 1, 17], [2, 4, 20, 177, 2, 17], [3, 4, 20,  
211, 2, 17], [4, 4, 20, 260, 2, 30], [5, 4, 20, 305, 2, 33], [6, 4, 20, 387, 3, 34], [7, 4, 20, 454, 8, 47], [8, 4, 20, 549, 10, 50], [9, 4, 20, 748,  
13, 52], [10, 4, 20, 930, 13, 66], [11, 4, 20, 1082, 14, 69], [12, 4, 20, 1360, 18, 75], [13, 4, 20, 1855, 19, 75], [14, 4, 20, 2315, 24, 75],  
[15, 4, 20, 2587, 26, 75], [16, 4, 20, 3054, 33, 91], [17, 4, 20, 3526, 40, 105], [18, 4, 20, 3954, 40, 126], [19, 4, 20, 4663, 49, 162], [20,  
4, 20, 5241, 49, 176], [21, 4, 20, 5959, 49, 179], [22, 4, 20, 6590, 56, 186], [23, 4, 20, 7278, 56, 186], [24, 4, 20, 7889, 66, 235], [25, 4,  
20, 8494, 69, 262], [26, 4, 20, 9070, 71, 272], [27, 4, 20, 9708, 71, 286], [28, 4, 20, 10231, 74, 311], [29, 4, 20, 10917, 90, 389], [30, 4,  
20, 11710, 93, 430], [1, 5, 20, 12507, 109, 458], [2, 5, 20, 13314, 109, 503], [3, 5, 20, 14136, 111, 507], [4, 5, 20, 14939, 111, 526], [5,  
5, 20, 15761, 127, 576], [6, 5, 20, 16590, 141, 611], [7, 5, 20, 17432, 156, 769], [8, 5, 20, 18350, 175, 813], [9, 5, 20, 19425, 186, 1030],  
[10, 5, 20, 20558, 195, 1236], [11, 5, 20, 21637, 209, 1389], [12, 5, 20, 22700, 219, 1582], [13, 5, 20, 23662, 226, 1745], [14, 5, 20,  
24580, 240, 1987], [15, 5, 20, 25525, 253, 2468], [16, 5, 20, 26462, 262, 2724], [17, 5, 20, 27369, 268, 3088], [18, 5, 20, 28290, 268,  
3361], [19, 5, 20, 29188, 271, 3614]]
```

dd := 7
Mosobl

```
T=[1, 1, 1, 3, 3, 4, 5, 8, 9, 11, 12, 17, 18, 35, 35, 35, 35, 41, 41, 49, 85, 112, 119, 119, 134, 177, 211, 260, 305, 387, 454, 549, 748, 930, 1082,
```

1360, 1855, 2315, 2587, 3054, 3526, 3954, 4663, 5241, 5959, 6590, 7278, 7889, 8494, 9070, 9708, 10231, 10917, 11710, 12507, 13314, 14136, 14939, 15761, 16590, 17432, 18350, 19425, 20558, 21637, 22700, 23662, 24580, 25525, 26462, 27369, 28290, 29188]

$T1 = [0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 2, 7, 7, 8, 8, 10, 10, 14, 17, 17, 17, 30, 33, 34, 47, 50, 52, 66, 69, 75, 75, 75, 75, 91, 105, 126, 162, 176, 179, 186, 186, 235, 262, 272, 286, 311, 389, 430, 458, 503, 507, 526, 576, 611, 769, 813, 1030, 1236, 1389, 1582, 1745, 1987, 2468, 2724, 3088, 3361, 3614]$

$T2 = [1, 1, 1, 3, 3, 4, 5, 8, 9, 11, 12, 17, 17, 34, 34, 34, 33, 34, 34, 41, 77, 102, 109, 105, 116, 158, 192, 228, 270, 350, 399, 489, 683, 851, 999, 1267, 1761, 2216, 2486, 2930, 3381, 3788, 4452, 5016, 5731, 6348, 7036, 7588, 8163, 8727, 9351, 9846, 10438, 11187, 11940, 12702, 13518, 14302, 15058, 15838, 16507, 17362, 18209, 19127, 20039, 20899, 21691, 22353, 22804, 23476, 24013, 24661, 25303]$

$T3 = [0, 1, 2, 2, 2, 2, 3, 8, 10, 13, 13, 14, 18, 19, 24, 26, 33, 40, 40, 49, 49, 49, 56, 56, 66, 69, 71, 71, 74, 90, 93, 109, 109, 111, 111, 127, 141, 156, 175, 186, 195, 209, 219, 226, 240, 253, 262, 268, 268, 271]$

73

[8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80]

(4)

> $h := x \rightarrow x;$

```
[seq(h(T[i]) - h(T[i-1]), i=2..nops(T))]; [seq(%[i] - %[i-1], i=2..nops(%))]; [seq(%[i] - %[i-1], i=2..nops(%))];
[seq([i+dd+1, %%%[i]], i=1..nops(%%%) )]: [seq([i+dd+2, %%%[i]], i=1..nops(%%%) )]: [seq([i+dd+3, %%%[i]], i=1..nops(%%%) )]:
display(
  plot([%%, %, %], style=point),
  plot([%%, %, %], legend=[`` , `` , `` ]),
  title=`      N[i]`, titlefont=[roman, 15], gridlines=true
);

[seq((h(T[i]) - h(T[i-5]))/5., i=6..nops(T))]: [seq((%[i] - %[i-3])/3., i=4..nops(%))]: [seq((%[i] - %[i-3])/3., i=4..nops(%))]:
[seq([i+dd+2, %%%[i]], i=1..nops(%%%) )]: [seq([i+dd+4, %%%[i]], i=1..nops(%%%) )]: [seq([i+dd+6, %%%[i]], i=1..nops(%%%) )]:
display(
  plot([%%, %, %], style=point),
  plot([%%, %, %], legend=[`` , `` , `` ]),
  title=`      N[i]`, titlefont=[roman, 15], gridlines=true
);
```

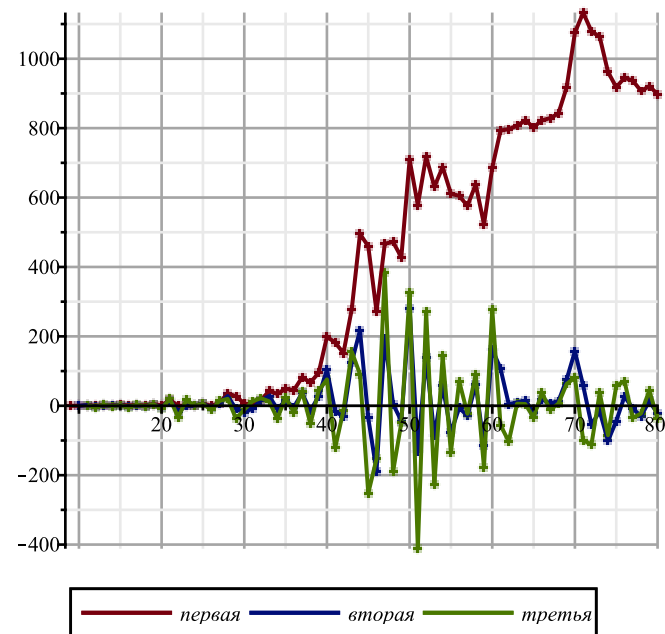
$h := x \mapsto x$

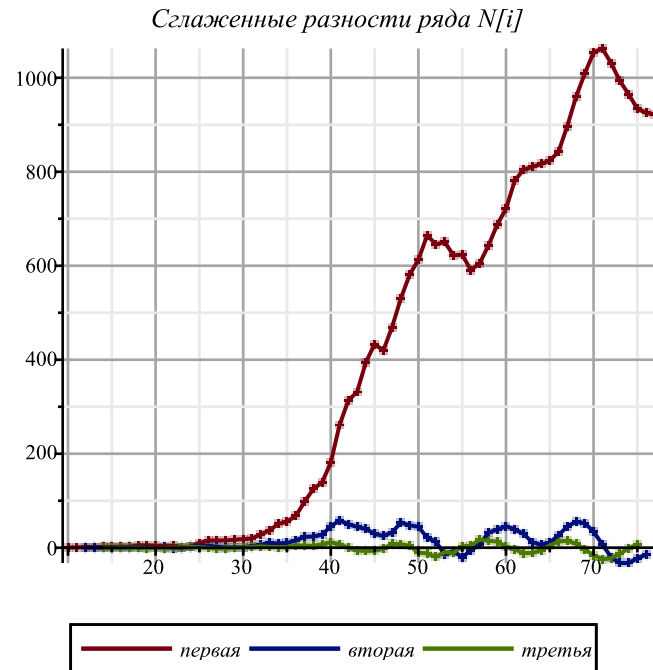
[0, 0, 2, 0, 1, 1, 3, 1, 2, 1, 5, 1, 17, 0, 0, 0, 6, 0, 8, 36, 27, 7, 0, 15, 43, 34, 49, 45, 82, 67, 95, 199, 182, 152, 278, 495, 460, 272, 467, 472, 428, 709, 578, 718, 631, 688, 611, 605, 576, 638, 523, 686, 793, 797, 807, 822, 803, 822, 829, 842, 918, 1075, 1133, 1079, 1063, 962, 918, 945, 937, 907, 921, 898]

[0, 2, -2, 1, 0, 2, -2, 1, -1, 4, -4, 16, -17, 0, 0, 6, -6, 8, 28, -9, -20, -7, 15, 28, -9, 15, -4, 37, -15, 28, 104, -17, -30, 126, 217, -35, -188, 195, 5, -44, 281, -131, 140, -87, 57, -77, -6, -29, 62, -115, 163, 107, 4, 10, 15, -19, 19, 7, 13, 76, 157, 58, -54, -16, -101, -44, 27, -8, -30, 14, -23]

[2, -4, 3, -1, 2, -4, 3, -2, 5, -8, 20, -33, 17, 0, 6, -12, 14, 20, -37, -11, 13, 22, 13, -37, 24, -19, 41, -52, 43, 76, -121, -13, 156, 91, -252, -153, 383, -190, -49, 325, -412, 271, -227, 144, -134, 71, -23, 91, -177, 278, -56, -103, 6, 5, -34, 38, -12, 6, 63, 81, -99, -112, 38, -85, 57, 71, -35, -22, 44, -37]

Разности ряда $N[i]$





```
> h:=x->ln(x);
```

```
[seq(h(T[i])-h(T[i-1]),i=2..nops(T)); [seq(%[i]-%[i-1],i=2..nops(%))]; [seq(%[i]-%[i-1],i=2..
nops(%))];
[seq([i+dd+1,%%[i]],i=1..nops(%%))]: [seq([i+dd+2,%%[i]],i=1..nops(%%))]: [seq([i+dd+3,%%[i]
],i=1..nops(%%))]:
display(
  plot([%%,%,%],style=point),
  plot([%%,%,%],legend=['`', '`', '`']),
  title=' ln(N[i]) ',titlefont=[roman,15] ,gridlines=true
);
```

```
[seq((h(T[i])-h(T[i-5]))/5.,i=6..nops(T)): [seq((%[i]-%[i-3])/3.,i=4..nops(%)): [seq((%[i]-%
[i-3])/3.,i=4..nops(%))]:
[seq([i+dd+2,%%[i]],i=1..nops(%%))]: [seq([i+dd+4,%%[i]],i=1..nops(%%))]: [seq([i+dd+6,%%[i]
],i=1..nops(%%))]:
display(
  plot([%%,%,%],style=point),
  plot([%%,%,%],legend=['`', '`', '`']),
```



```
title = `
```

```
ln(N[i])`,titlefont=[roman,15],gridlines=true
```

```
);
```

$$h := x \mapsto \ln(x)$$

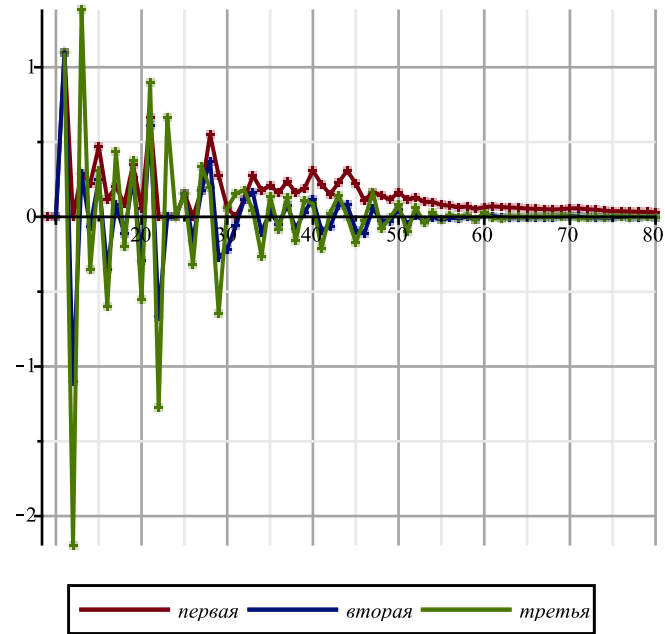
```
[0, 0, ln(3), 0, 2 ln(2) - ln(3), ln(5) - 2 ln(2), 3 ln(2) - ln(5), 2 ln(3) - 3 ln(2), ln(11) - 2 ln(3), ln(12) - ln(11), ln(17) - ln(12),  
ln(18) - ln(17), ln(35) - ln(18), 0, 0, 0, ln(41) - ln(35), 0, 2 ln(7) - ln(41), ln(85) - 2 ln(7), ln(112) - ln(85), ln(119)  
- ln(112), 0, ln(134) - ln(119), ln(177) - ln(134), ln(211) - ln(177), ln(260) - ln(211), ln(305) - ln(260), ln(387) - ln(305),  
ln(454) - ln(387), ln(549) - ln(454), ln(748) - ln(549), ln(930) - ln(748), ln(1082) - ln(930), ln(1360) - ln(1082), ln(1855)  
- ln(1360), ln(2315) - ln(1855), ln(2587) - ln(2315), ln(3054) - ln(2587), ln(3526) - ln(3054), ln(3954) - ln(3526), ln(4663)  
- ln(3954), ln(5241) - ln(4663), ln(5959) - ln(5241), ln(6590) - ln(5959), ln(7278) - ln(6590), ln(7889) - ln(7278), ln(8494)  
- ln(7889), ln(9070) - ln(8494), ln(9708) - ln(9070), ln(10231) - ln(9708), ln(10917) - ln(10231), ln(11710) - ln(10917),  
ln(12507) - ln(11710), ln(13314) - ln(12507), ln(14136) - ln(13314), ln(14939) - ln(14136), ln(15761) - ln(14939), ln(16590)  
- ln(15761), ln(17432) - ln(16590), ln(18350) - ln(17432), ln(19425) - ln(18350), ln(20558) - ln(19425), ln(21637)  
- ln(20558), ln(22700) - ln(21637), ln(23662) - ln(22700), ln(24580) - ln(23662), ln(25525) - ln(24580), ln(26462)  
- ln(25525), ln(27369) - ln(26462), ln(28290) - ln(27369), ln(29188) - ln(28290) ]
```

```
[0, ln(3), -ln(3), 2 ln(2) - ln(3), ln(5) - 4 ln(2) + ln(3), 5 ln(2) - 2 ln(5), 2 ln(3) - 6 ln(2) + ln(5), ln(11) - 4 ln(3) + 3 ln(2),  
ln(12) - 2 ln(11) + 2 ln(3), ln(17) - 2 ln(12) + ln(11), ln(18) - 2 ln(17) + ln(12), ln(35) - 2 ln(18) + ln(17), -ln(35) + ln(18),  
0, 0, ln(41) - ln(35), -ln(41) + ln(35), 2 ln(7) - ln(41), ln(85) - 4 ln(7) + ln(41), ln(112) - 2 ln(85) + 2 ln(7), ln(119)  
- 2 ln(112) + ln(85), -ln(119) + ln(112), ln(134) - ln(119), ln(177) - 2 ln(134) + ln(119), ln(211) - 2 ln(177) + ln(134),  
ln(260) - 2 ln(211) + ln(177), ln(305) - 2 ln(260) + ln(211), ln(387) - 2 ln(305) + ln(260), ln(454) - 2 ln(387) + ln(305),  
ln(549) - 2 ln(454) + ln(387), ln(748) - 2 ln(549) + ln(454), ln(930) - 2 ln(748) + ln(549), ln(1082) - 2 ln(930) + ln(748),  
ln(1360) - 2 ln(1082) + ln(930), ln(1855) - 2 ln(1360) + ln(1082), ln(2315) - 2 ln(1855) + ln(1360), ln(2587) - 2 ln(2315)  
+ ln(1855), ln(3054) - 2 ln(2587) + ln(2315), ln(3526) - 2 ln(3054) + ln(2587), ln(3954) - 2 ln(3526) + ln(3054), ln(4663)  
- 2 ln(3954) + ln(3526), ln(5241) - 2 ln(4663) + ln(3954), ln(5959) - 2 ln(5241) + ln(4663), ln(6590) - 2 ln(5959)  
+ ln(5241), ln(7278) - 2 ln(6590) + ln(5959), ln(7889) - 2 ln(7278) + ln(6590), ln(8494) - 2 ln(7889) + ln(7278), ln(9070)  
- 2 ln(8494) + ln(7889), ln(9708) - 2 ln(9070) + ln(8494), ln(10231) - 2 ln(9708) + ln(9070), ln(10917) - 2 ln(10231)  
+ ln(9708), ln(11710) - 2 ln(10917) + ln(10231), ln(12507) - 2 ln(11710) + ln(10917), ln(13314) - 2 ln(12507) + ln(11710),  
ln(14136) - 2 ln(13314) + ln(12507), ln(14939) - 2 ln(14136) + ln(13314), ln(15761) - 2 ln(14939) + ln(14136), ln(16590)  
- 2 ln(15761) + ln(14939), ln(17432) - 2 ln(16590) + ln(15761), ln(18350) - 2 ln(17432) + ln(16590), ln(19425) - 2 ln(18350)  
+ ln(17432), ln(20558) - 2 ln(19425) + ln(18350), ln(21637) - 2 ln(20558) + ln(19425), ln(22700) - 2 ln(21637) + ln(20558),  
ln(23662) - 2 ln(22700) + ln(21637), ln(24580) - 2 ln(23662) + ln(22700), ln(25525) - 2 ln(24580) + ln(23662), ln(26462)
```

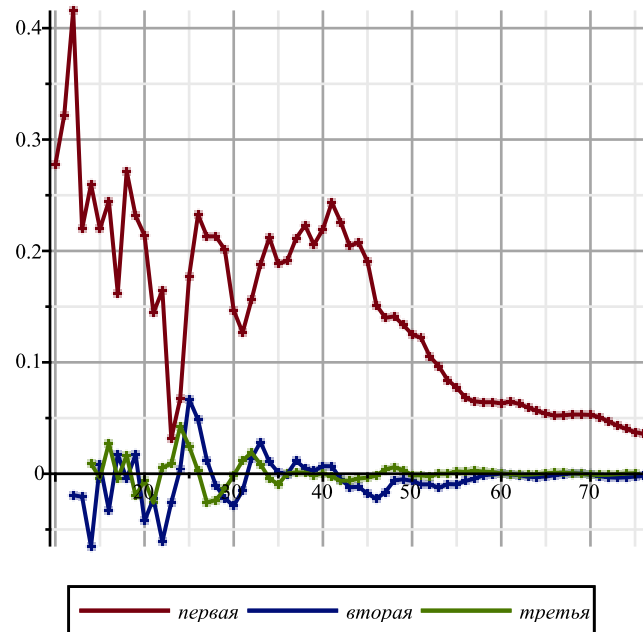
$-2 \ln(25525) + \ln(24580), \ln(27369) - 2 \ln(26462) + \ln(25525), \ln(28290) - 2 \ln(27369) + \ln(26462), \ln(29188) - 2 \ln(28290) + \ln(27369)]$

$[\ln(3), -2 \ln(3), 2 \ln(2), 2 \ln(3) - 6 \ln(2) + \ln(5), 9 \ln(2) - 3 \ln(5) - \ln(3), 2 \ln(3) - 11 \ln(2) + 3 \ln(5), \ln(11) - 6 \ln(3) + 9 \ln(2) - \ln(5), \ln(12) - 3 \ln(11) + 6 \ln(3) - 3 \ln(2), \ln(17) - 3 \ln(12) + 3 \ln(11) - 2 \ln(3), \ln(18) - 3 \ln(17) + 3 \ln(12) - \ln(11), \ln(35) - 3 \ln(18) + 3 \ln(17) - \ln(12), -2 \ln(35) + 3 \ln(18) - \ln(17), \ln(35) - \ln(18), 0, \ln(41) - \ln(35), -2 \ln(41) + 2 \ln(35), 2 \ln(7) - \ln(35), \ln(85) - 6 \ln(7) + 2 \ln(41), \ln(112) - 3 \ln(85) + 6 \ln(7) - \ln(41), \ln(119) - 3 \ln(112) + 3 \ln(85) - 2 \ln(7), -2 \ln(119) + 3 \ln(112) - \ln(85), \ln(134) - \ln(112), \ln(177) - 3 \ln(134) + 2 \ln(119), \ln(211) - 3 \ln(177) + 3 \ln(134) - \ln(119), \ln(260) - 3 \ln(211) + 3 \ln(177) - \ln(134), \ln(305) - 3 \ln(260) + 3 \ln(211) - \ln(177), \ln(387) - 3 \ln(305) + 3 \ln(260) - \ln(211), \ln(454) - 3 \ln(387) + 3 \ln(305) - \ln(260), \ln(549) - 3 \ln(454) + 3 \ln(387) - \ln(305), \ln(748) - 3 \ln(549) + 3 \ln(454) - \ln(387), \ln(930) - 3 \ln(748) + 3 \ln(549) - \ln(454), \ln(1082) - 3 \ln(930) + 3 \ln(748) - \ln(549), \ln(1360) - 3 \ln(1082) + 3 \ln(930) - \ln(748), \ln(1855) - 3 \ln(1360) + 3 \ln(1082) - \ln(930), \ln(2315) - 3 \ln(1855) + 3 \ln(1360) - \ln(1082), \ln(2587) - 3 \ln(2315) + 3 \ln(1855) - \ln(1360), \ln(3054) - 3 \ln(2587) + 3 \ln(2315) - \ln(1855), \ln(3526) - 3 \ln(3054) + 3 \ln(2587) - \ln(2315), \ln(3954) - 3 \ln(3526) + 3 \ln(3054) - \ln(2587), \ln(4663) - 3 \ln(3954) + 3 \ln(3526) - \ln(3054), \ln(5241) - 3 \ln(4663) + 3 \ln(3954) - \ln(3526), \ln(5959) - 3 \ln(5241) + 3 \ln(4663) - \ln(3954), \ln(6590) - 3 \ln(5959) + 3 \ln(5241) - \ln(4663), \ln(7278) - 3 \ln(6590) + 3 \ln(5959) - \ln(5241), \ln(7889) - 3 \ln(7278) + 3 \ln(6590) - \ln(5959), \ln(8494) - 3 \ln(7889) + 3 \ln(7278) - \ln(6590), \ln(9070) - 3 \ln(8494) + 3 \ln(7889) - \ln(7278), \ln(9708) - 3 \ln(9070) + 3 \ln(8494) - \ln(7889), \ln(10231) - 3 \ln(9708) + 3 \ln(9070) - \ln(8494), \ln(10917) - 3 \ln(10231) + 3 \ln(9708) - \ln(9070), \ln(11710) - 3 \ln(10917) + 3 \ln(10231) - \ln(9708), \ln(12507) - 3 \ln(11710) + 3 \ln(10917) - \ln(10231), \ln(13314) - 3 \ln(12507) + 3 \ln(11710) - \ln(10917), \ln(14136) - 3 \ln(13314) + 3 \ln(12507) - \ln(11710), \ln(14939) - 3 \ln(14136) + 3 \ln(13314) - \ln(12507), \ln(15761) - 3 \ln(14939) + 3 \ln(14136) - \ln(13314), \ln(16590) - 3 \ln(15761) + 3 \ln(14939) - \ln(14136), \ln(17432) - 3 \ln(16590) + 3 \ln(15761) - \ln(14939), \ln(18350) - 3 \ln(17432) + 3 \ln(16590) - \ln(15761), \ln(19425) - 3 \ln(18350) + 3 \ln(17432) - \ln(16590), \ln(20558) - 3 \ln(19425) + 3 \ln(18350) - \ln(17432), \ln(21637) - 3 \ln(20558) + 3 \ln(19425) - \ln(18350), \ln(22700) - 3 \ln(21637) + 3 \ln(20558) - \ln(19425), \ln(23662) - 3 \ln(22700) + 3 \ln(21637) - \ln(20558), \ln(24580) - 3 \ln(23662) + 3 \ln(22700) - \ln(21637), \ln(25525) - 3 \ln(24580) + 3 \ln(23662) - \ln(22700), \ln(26462) - 3 \ln(25525) + 3 \ln(24580) - \ln(23662), \ln(27369) - 3 \ln(26462) + 3 \ln(25525) - \ln(24580), \ln(28290) - 3 \ln(27369) + 3 \ln(26462) - \ln(25525), \ln(29188) - 3 \ln(28290) + 3 \ln(27369) - \ln(26462)]$

Разности ряда $\ln(N[i])$



Сглаженные разности ряда $\ln(N[i])$



```
> h:=x->ln(x);
```

```
[seq(h(T[i])-h(T[i-1]),i=2..nops(T)); [seq(%[i]-%[i-1],i=2..nops(%))]; [seq(%[i]-%[i-1],i=2..
nops(%))];
[seq([i+dd+1,%%[i]],i=1..nops(%%))]: [seq([i+dd+1,%%[i]],i=1..nops(%%))]: [seq([i+dd+1,%%[i]
],i=1..nops(%%))]:
display(
plot([%%,%,%],style=point),
plot([%%,%,%],legend=['`','`','`']),
title=' ln(N[i]) ',titlefont=[roman,15] ,gridlines=true
);
```

$$h := x \mapsto \ln(x)$$

```
[0, 0, ln(3), 0, 2 ln(2) - ln(3), ln(5) - 2 ln(2), 3 ln(2) - ln(5), 2 ln(3) - 3 ln(2), ln(11) - 2 ln(3), ln(12) - ln(11), ln(17) - ln(12),
ln(18) - ln(17), ln(35) - ln(18), 0, 0, 0, ln(41) - ln(35), 0, 2 ln(7) - ln(41), ln(85) - 2 ln(7), ln(112) - ln(85), ln(119)
- ln(112), 0, ln(134) - ln(119), ln(177) - ln(134), ln(211) - ln(177), ln(260) - ln(211), ln(305) - ln(260), ln(387) - ln(305),
ln(454) - ln(387), ln(549) - ln(454), ln(748) - ln(549), ln(930) - ln(748), ln(1082) - ln(930), ln(1360) - ln(1082), ln(1855)
```

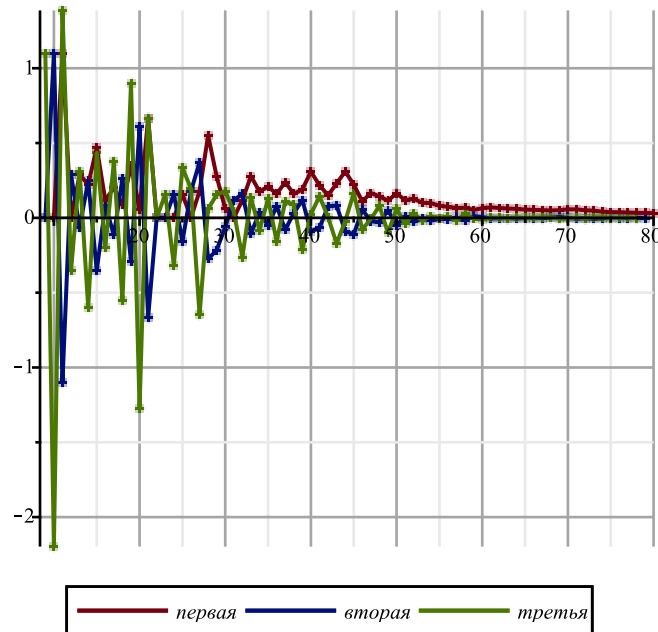
$-\ln(1360), \ln(2315) - \ln(1855), \ln(2587) - \ln(2315), \ln(3054) - \ln(2587), \ln(3526) - \ln(3054), \ln(3954) - \ln(3526), \ln(4663) - \ln(3954), \ln(5241) - \ln(4663), \ln(5959) - \ln(5241), \ln(6590) - \ln(5959), \ln(7278) - \ln(6590), \ln(7889) - \ln(7278), \ln(8494) - \ln(7889), \ln(9070) - \ln(8494), \ln(9708) - \ln(9070), \ln(10231) - \ln(9708), \ln(10917) - \ln(10231), \ln(11710) - \ln(10917), \ln(12507) - \ln(11710), \ln(13314) - \ln(12507), \ln(14136) - \ln(13314), \ln(14939) - \ln(14136), \ln(15761) - \ln(14939), \ln(16590) - \ln(15761), \ln(17432) - \ln(16590), \ln(18350) - \ln(17432), \ln(19425) - \ln(18350), \ln(20558) - \ln(19425), \ln(21637) - \ln(20558), \ln(22700) - \ln(21637), \ln(23662) - \ln(22700), \ln(24580) - \ln(23662), \ln(25525) - \ln(24580), \ln(26462) - \ln(25525), \ln(27369) - \ln(26462), \ln(28290) - \ln(27369), \ln(29188) - \ln(28290)]$

$[0, \ln(3), -\ln(3), 2 \ln(2) - \ln(3), \ln(5) - 4 \ln(2) + \ln(3), 5 \ln(2) - 2 \ln(5), 2 \ln(3) - 6 \ln(2) + \ln(5), \ln(11) - 4 \ln(3) + 3 \ln(2), \ln(12) - 2 \ln(11) + 2 \ln(3), \ln(17) - 2 \ln(12) + \ln(11), \ln(18) - 2 \ln(17) + \ln(12), \ln(35) - 2 \ln(18) + \ln(17), -\ln(35) + \ln(18), 0, 0, \ln(41) - \ln(35), -\ln(41) + \ln(35), 2 \ln(7) - \ln(41), \ln(85) - 4 \ln(7) + \ln(41), \ln(112) - 2 \ln(85) + 2 \ln(7), \ln(119) - 2 \ln(112) + \ln(85), -\ln(119) + \ln(112), \ln(134) - \ln(119), \ln(177) - 2 \ln(134) + \ln(119), \ln(211) - 2 \ln(177) + \ln(134), \ln(260) - 2 \ln(211) + \ln(177), \ln(305) - 2 \ln(260) + \ln(211), \ln(387) - 2 \ln(305) + \ln(260), \ln(454) - 2 \ln(387) + \ln(305), \ln(549) - 2 \ln(454) + \ln(387), \ln(748) - 2 \ln(549) + \ln(454), \ln(930) - 2 \ln(748) + \ln(549), \ln(1082) - 2 \ln(930) + \ln(748), \ln(1360) - 2 \ln(1082) + \ln(930), \ln(1855) - 2 \ln(1360) + \ln(1082), \ln(2315) - 2 \ln(1855) + \ln(1360), \ln(2587) - 2 \ln(2315) + \ln(1855), \ln(3054) - 2 \ln(2587) + \ln(2315), \ln(3526) - 2 \ln(3054) + \ln(2587), \ln(3954) - 2 \ln(3526) + \ln(3054), \ln(4663) - 2 \ln(3954) + \ln(3526), \ln(5241) - 2 \ln(4663) + \ln(3954), \ln(5959) - 2 \ln(5241) + \ln(4663), \ln(6590) - 2 \ln(5959) + \ln(5241), \ln(7278) - 2 \ln(6590) + \ln(5959), \ln(7889) - 2 \ln(7278) + \ln(6590), \ln(8494) - 2 \ln(7889) + \ln(7278), \ln(9070) - 2 \ln(8494) + \ln(7889), \ln(9708) - 2 \ln(9070) + \ln(8494), \ln(10231) - 2 \ln(9708) + \ln(9070), \ln(10917) - 2 \ln(10231) + \ln(9708), \ln(11710) - 2 \ln(10917) + \ln(10231), \ln(12507) - 2 \ln(11710) + \ln(10917), \ln(13314) - 2 \ln(12507) + \ln(11710), \ln(14136) - 2 \ln(13314) + \ln(12507), \ln(14939) - 2 \ln(14136) + \ln(13314), \ln(15761) - 2 \ln(14939) + \ln(14136), \ln(16590) - 2 \ln(15761) + \ln(14939), \ln(17432) - 2 \ln(16590) + \ln(15761), \ln(18350) - 2 \ln(17432) + \ln(16590), \ln(19425) - 2 \ln(18350) + \ln(17432), \ln(20558) - 2 \ln(19425) + \ln(18350), \ln(21637) - 2 \ln(20558) + \ln(19425), \ln(22700) - 2 \ln(21637) + \ln(20558), \ln(23662) - 2 \ln(22700) + \ln(21637), \ln(24580) - 2 \ln(23662) + \ln(22700), \ln(25525) - 2 \ln(24580) + \ln(23662), \ln(26462) - 2 \ln(25525) + \ln(24580), \ln(27369) - 2 \ln(26462) + \ln(25525), \ln(28290) - 2 \ln(27369) + \ln(26462), \ln(29188) - 2 \ln(28290) + \ln(27369)]$

$[\ln(3), -2 \ln(3), 2 \ln(2), 2 \ln(3) - 6 \ln(2) + \ln(5), 9 \ln(2) - 3 \ln(5) - \ln(3), 2 \ln(3) - 11 \ln(2) + 3 \ln(5), \ln(11) - 6 \ln(3) + 9 \ln(2) - \ln(5), \ln(12) - 3 \ln(11) + 6 \ln(3) - 3 \ln(2), \ln(17) - 3 \ln(12) + 3 \ln(11) - 2 \ln(3), \ln(18) - 3 \ln(17) + 3 \ln(12) - \ln(11), \ln(35) - 3 \ln(18) + 3 \ln(17) - \ln(12), -2 \ln(35) + 3 \ln(18) - \ln(17), \ln(35) - \ln(18), 0, \ln(41) - \ln(35), -2 \ln(41) + 2 \ln(35), 2 \ln(7) - \ln(35), \ln(85) - 6 \ln(7) + 2 \ln(41), \ln(112) - 3 \ln(85) + 6 \ln(7) - \ln(41), \ln(119) - 3 \ln(112) + 3 \ln(85) - 2 \ln(7), -2 \ln(119) + 3 \ln(112) - \ln(85), \ln(134) - \ln(112), \ln(177) - 3 \ln(134) + 2 \ln(119), \ln(211) - 3 \ln(177) + 3 \ln(134) - \ln(119),$

$\ln(260) - 3 \ln(211) + 3 \ln(177) - \ln(134), \ln(305) - 3 \ln(260) + 3 \ln(211) - \ln(177), \ln(387) - 3 \ln(305) + 3 \ln(260)$
 $- \ln(211), \ln(454) - 3 \ln(387) + 3 \ln(305) - \ln(260), \ln(549) - 3 \ln(454) + 3 \ln(387) - \ln(305), \ln(748) - 3 \ln(549) + 3 \ln(454)$
 $- \ln(387), \ln(930) - 3 \ln(748) + 3 \ln(549) - \ln(454), \ln(1082) - 3 \ln(930) + 3 \ln(748) - \ln(549), \ln(1360) - 3 \ln(1082)$
 $+ 3 \ln(930) - \ln(748), \ln(1855) - 3 \ln(1360) + 3 \ln(1082) - \ln(930), \ln(2315) - 3 \ln(1855) + 3 \ln(1360) - \ln(1082), \ln(2587)$
 $- 3 \ln(2315) + 3 \ln(1855) - \ln(1360), \ln(3054) - 3 \ln(2587) + 3 \ln(2315) - \ln(1855), \ln(3526) - 3 \ln(3054) + 3 \ln(2587)$
 $- \ln(2315), \ln(3954) - 3 \ln(3526) + 3 \ln(3054) - \ln(2587), \ln(4663) - 3 \ln(3954) + 3 \ln(3526) - \ln(3054), \ln(5241)$
 $- 3 \ln(4663) + 3 \ln(3954) - \ln(3526), \ln(5959) - 3 \ln(5241) + 3 \ln(4663) - \ln(3954), \ln(6590) - 3 \ln(5959) + 3 \ln(5241)$
 $- \ln(4663), \ln(7278) - 3 \ln(6590) + 3 \ln(5959) - \ln(5241), \ln(7889) - 3 \ln(7278) + 3 \ln(6590) - \ln(5959), \ln(8494)$
 $- 3 \ln(7889) + 3 \ln(7278) - \ln(6590), \ln(9070) - 3 \ln(8494) + 3 \ln(7889) - \ln(7278), \ln(9708) - 3 \ln(9070) + 3 \ln(8494)$
 $- \ln(7889), \ln(10231) - 3 \ln(9708) + 3 \ln(9070) - \ln(8494), \ln(10917) - 3 \ln(10231) + 3 \ln(9708) - \ln(9070), \ln(11710)$
 $- 3 \ln(10917) + 3 \ln(10231) - \ln(9708), \ln(12507) - 3 \ln(11710) + 3 \ln(10917) - \ln(10231), \ln(13314) - 3 \ln(12507)$
 $+ 3 \ln(11710) - \ln(10917), \ln(14136) - 3 \ln(13314) + 3 \ln(12507) - \ln(11710), \ln(14939) - 3 \ln(14136) + 3 \ln(13314)$
 $- \ln(12507), \ln(15761) - 3 \ln(14939) + 3 \ln(14136) - \ln(13314), \ln(16590) - 3 \ln(15761) + 3 \ln(14939) - \ln(14136), \ln(17432)$
 $- 3 \ln(16590) + 3 \ln(15761) - \ln(14939), \ln(18350) - 3 \ln(17432) + 3 \ln(16590) - \ln(15761), \ln(19425) - 3 \ln(18350)$
 $+ 3 \ln(17432) - \ln(16590), \ln(20558) - 3 \ln(19425) + 3 \ln(18350) - \ln(17432), \ln(21637) - 3 \ln(20558) + 3 \ln(19425)$
 $- \ln(18350), \ln(22700) - 3 \ln(21637) + 3 \ln(20558) - \ln(19425), \ln(23662) - 3 \ln(22700) + 3 \ln(21637) - \ln(20558), \ln(24580)$
 $- 3 \ln(23662) + 3 \ln(22700) - \ln(21637), \ln(25525) - 3 \ln(24580) + 3 \ln(23662) - \ln(22700), \ln(26462) - 3 \ln(25525)$
 $+ 3 \ln(24580) - \ln(23662), \ln(27369) - 3 \ln(26462) + 3 \ln(25525) - \ln(24580), \ln(28290) - 3 \ln(27369) + 3 \ln(26462)$
 $- \ln(25525), \ln(29188) - 3 \ln(28290) + 3 \ln(27369) - \ln(26462)]$

Разности ряда $\ln(N[i])$



```
> n:=1: ne:=n: 'f(t)'=Sum(a[j]*t^j,j=0..n);
```

```
fM:=proc(x) global M,chi2,F,T,f_; M:=x; chi2(T,F(T,chi2,f_)); end:
```

```
` `; `Approximation of the infection schedule by the solution of the Verhulst equation`; ` `;
```

```
M:=goldMin(fM,max(T)+2..max(T)*2,1);
```

```
nu:=F(T,chi2,f_): f:=unapply(ff(%(t)),t): N(t)=%(t); Chi2:=chi2(T,%%);
```

```
cat(`Next day forecast: ` ,round(f(nops(T)+1)));
```

```
cat(`The level of 0.5 M is reached at ` ,round(1+fsolve(f(d)=0.5*M,d=30)+dd-31), ` apr`);
```

```
cat(`The level of 0.85 M is reached at ` ,round(1+fsolve(f(d)=0.85*M,d=30)+dd-31), ` apr`);
```

```
` `; `Approximation of the infection schedule by solving the Malthus equation`; ` `;
```

```
nue:=F(T,chi2e,f_): fe:=unapply(ff(%(t)),t): N(t)=%(t);
```

```
simplify([diff(nu(d-dd),d),diff(nue(d-dd),d)]: [coeff(%[1],d,i) $ i=0..n-1];
```

```
plot(%%,d=1+dd..nops(T)+dd,view=[0..nops(T)+dd,0..0.5],legend=[` ` , ` `],
```

```
linestyle=[solid,dash],title=` ` ,titlefont=[roman,20],labels=[t,alpha(t)],
```

```
gridlines=true);
```

```
d1:=fsolve(f(d)=0.5*M,d=30)+dd; K_:=M; alpha_:=coeff(nu(t),t,1);
```

```

n:=4: ne:=n: 'f(t)'=Sum(a[j]*t^j,j=0..n);

fM:=proc(x) global M,chi2,F,T,f_; M:=x; chi2(T,F(T,chi2,f_)); end:

``; `Approximation of the infection schedule by the solution of the Verhulst equation`; ``;
M:=goldMin(fM,max(T)+2..max(T)*2,1);
nu:=F(T,chi2,f_): f:=unapply(ff(%(t)),t): N(t)=%(t); Chi2:=chi2(T,%%);
cat(`Next day forecast:`,round(f(nops(T)+1)));
cat(`The level of 0.5 M is reached at`,round(1+fsolve(f(d)=0.5*M,d=30)+dd-31),` apr`);
cat(`The level of 0.85 M is reached at`,round(1+fsolve(f(d)=0.85*M,d=30)+dd-31),` apr`);
``; `Approximation of the infection schedule by solving the Malthus equation`; ``;
nue:=F(T,chi2e,f_): fe:=unapply(fffe(%(t)),t): N(t)=%(t);

[seq([i,(
(T[i-dd]-T[i-dd-1])/(T2[i-dd]+T2[i-dd-1])/((1-T[i-dd]/M)+(1-T[i-dd-1]/M))
)*4],i=1+dd+1..nops(T)+dd): [seq([%[i][1],(%[i-1][2]+[%i][2]+[%i+1][2])/3],i=2..nops(%)-1)]:
Palpha:=display(plot([%],color=blue),plot([%],style=point,symbolsize=8,symbol=solidcircle,color=
blue)):

simplify([diff(nu(d-dd),d),diff(nue(d-dd),d)]): [coeff(%[1],d,i) $ i=0..n-1];
plot(%%,d=1+dd..nops(T)+dd,view=[0..nops(T)+dd,0..0.5],legend=[``,``],
linestyle=[solid,dash],title=`,titlefont=[roman,20],labels=[t,alpha(t)],
gridlines=true):

display(Palpha,%);

```

$$f(t) = \sum_{j=0}^1 a_j t^j$$

Approximation of the infection schedule by the solution of the Verhulst equation

$$M := 29190.36848$$

$$N(t) = 29190.36848 - \frac{29190.36848}{e^{0.1377192299t - 7.795966363} + 1}$$

$Chi2 := 4995.557242$

Next day forecast: 26752

The level of 0.5 M is reached at 34 apr

The level of 0.85 M is reached at 46 apr

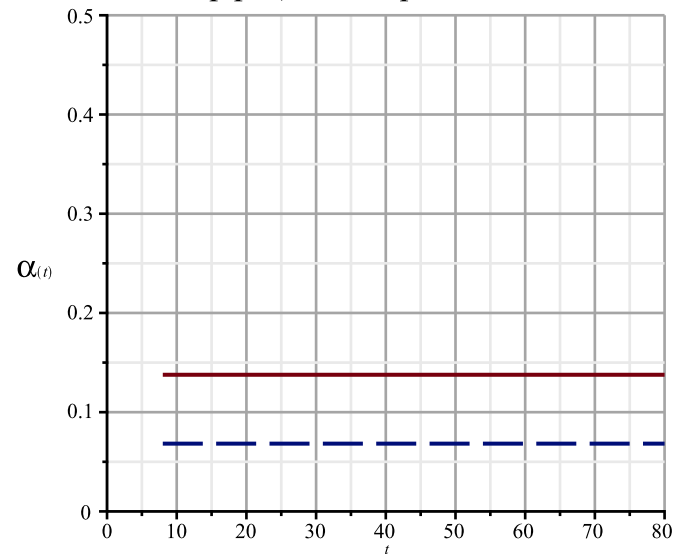
``

Approximation of the infection schedule by solving the Malthus equation

``

$$N(t) = e^{0.06829885811 t + 5.506105097} [0.1377192299]$$

Коэффициент заражения



Ферхольст Мальтус

$dI := 63.60768194$

$K_ := 29190.36848$

$alpha_ := 0.1377192299$

$$f(t) = \sum_{j=0}^4 a_j t^j$$

Approximation of the infection schedule by the solution of the Verhulst equation

$$M := 30675.24014$$

$$N(t) = 30675.24014 - \frac{30675.24014}{e^{3.085613677 \cdot 10^{-6} t^4 - 0.0005033785700 t^3 + 0.02718989511 t^2 - 0.3785226257 t - 6.271787470} + 1}$$

$$Chi2 := 334.9471548$$

Next day forecast: 29421

The level of 0.5 M is reached at -32 apr

The level of 0.85 M is reached at 46 apr

Approximation of the infection schedule by solving the Malthus equation

$$N(t) = e^{9.107351936 \cdot 10^{-7} t^4 - 0.0001506683805 t^3 + 0.006302094212 t^2 + 0.1302513311 t - 0.01779454360}$$

[-0.837411269000000, 0.0773360310000000, -0.00176932725900000, 0.00001234245471]



```

> df:=unapply(diff(f(i),i),i): ddf:=unapply(diff(f(i),i,i),i):

display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=10,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(90,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(90,dd+nops(T))),
  seq(plot([[i+dd,T[i]+3*sqrt(T[i])],[i+dd,T[i]-3*sqrt(T[i])]],color=blue),i=1..nops(T)),
  axis[2]=[mode=log],
  view=[1..80,1..M*1.1],labels=[t,N(t)],gridlines=true
);

display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=8,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(120,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(120,dd+nops(T))),
  # seq(plot([[i+dd,T[i]+3*sqrt(T[i])],[i+dd,T[i]-3*sqrt(T[i])]],color=blue),i=1..nops(T)),
  axis[2]=[mode=log],
  view=[1..nops(T)+dd+1,1..T[nops(T)]*1.1],labels=[t,N(t)],gridlines=true
);

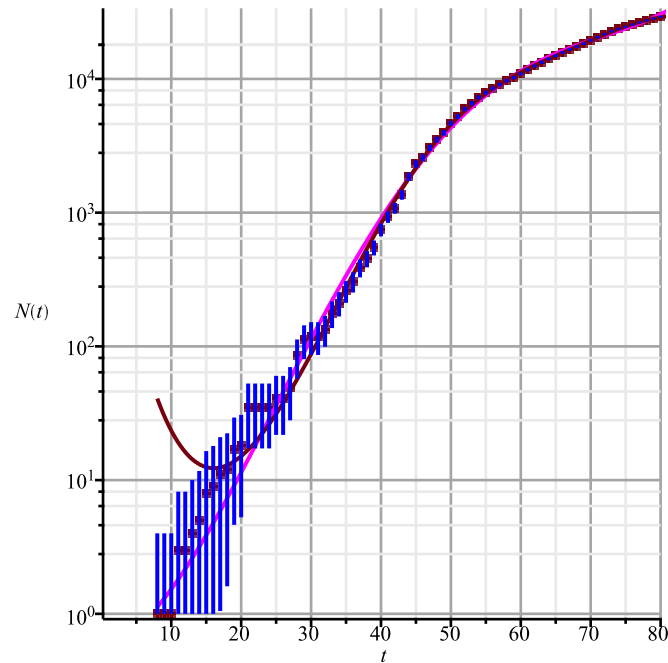
```

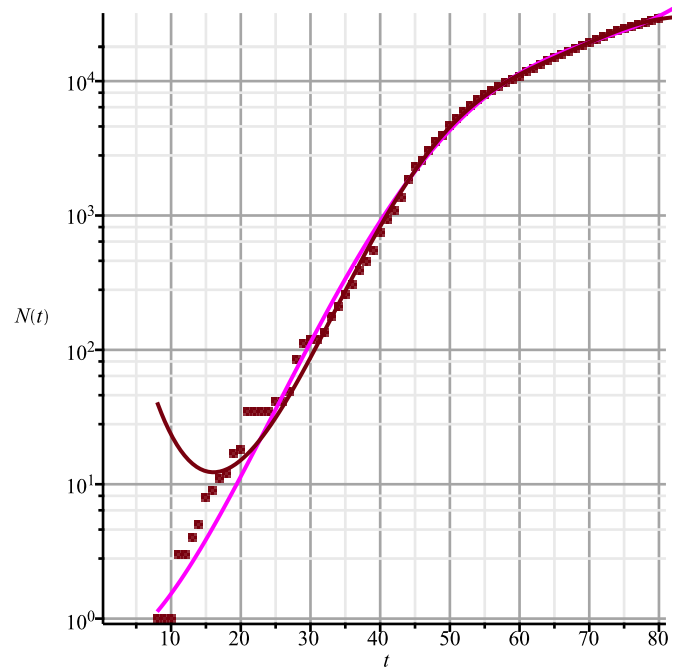
```

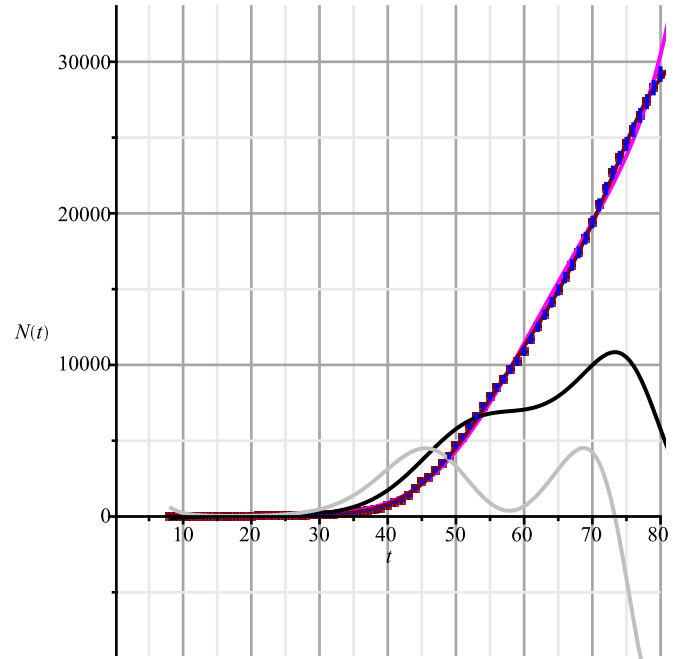
display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=10,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(120,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(dd+nops(T),90)),
  plot(10*df(i-dd),i=1+dd..max(dd+nops(T),120),color=black),
  plot(100*ddf(i-dd),i=1+dd..max(dd+nops(T),120),color=gray),
  seq(plot([[i+dd,T[i]+3*sqrt(T[i])],[i+dd,T[i]-3*sqrt(T[i])]],color=blue),i=1..nops(T)),
  view=[1..80,-M*0.3..M*1.1],labels=[t,N(t)],gridlines=true
);

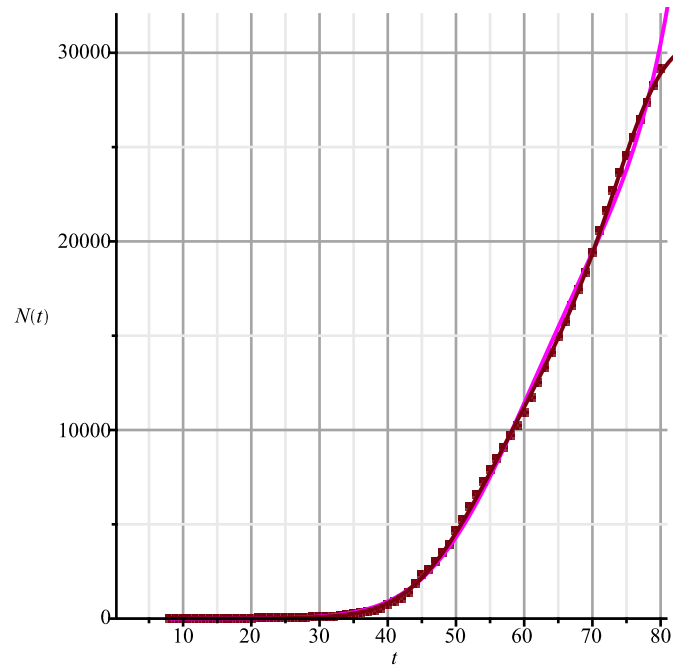
display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=8,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(120,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(dd+nops(T),120)),
  # seq(plot([[i+dd,T[i]+3*sqrt(T[i])],[i+dd,T[i]-3*sqrt(T[i])]],color=blue),i=1..nops(T)),
  view=[1..nops(T)+dd+1,1..T[nops(T)]*1.1],labels=[t,N(t)],gridlines=true
);

```



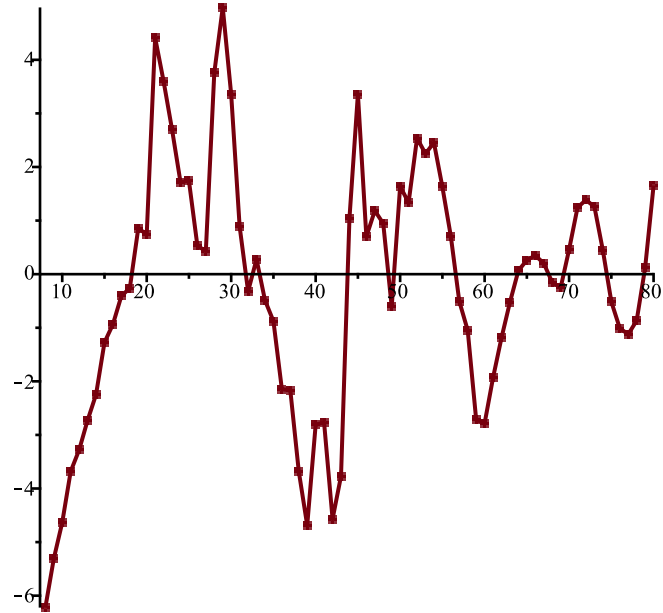






```
> dT:=[[i, (T[i-dd]-f(i-dd))/sigma(f(i-dd))] $ i=1+dd..dd+nops(T)]:
display( plot(%), plot(% ,style=point,symbolsize=8,symbol=solidcircle),title = ` ` ,titlefont=
[roman,20] );
```

Девияция



```
> ===== ` ;  
`FORECAST` ;  
===== ` ;
```

=====
FORECAST
=====

```
> proc3:=proc (E)  
  E[1]*convert (map (X->X^coeff (E[2] ,X,1) ,M) , `*` ) ;  
end:  
  
proc2:=proc (X,E)  
  proc3 (E) * (coeff (E[3] ,X,1) -coeff (E[2] ,X,1)) ;  
end:  
  
proc1:=proc (X)  
  convert (map (E->proc2 (X,E) ,L) , `+` ) ;  
end:
```



```

> A:='A': B:='B': C:='C': M:=[A,B,C];

L:=
 [P[`01`],0,A],
 [(B/K)*P[`12`],A,B],
 [P[`23`],B,C],
 [P[`10`],A,0], [P[`20`],B,0], [P[`30`],C,0]
]: Matrix(%);

eqs:=map(X->Diff(X,t)=procl(X),M); Vector(%);

```

$$M := [A, B, C]$$

$$\begin{bmatrix} P_{01} & 0 & A \\ \frac{BP_{12}}{K} & A & B \\ P_{23} & B & C \\ P_{10} & A & 0 \\ P_{20} & B & 0 \\ P_{30} & C & 0 \end{bmatrix}$$

$$eqs := \left[\frac{\partial}{\partial t} A = P_{01} - \frac{BP_{12}A}{K} - P_{10}A, \frac{\partial}{\partial t} B = \frac{BP_{12}A}{K} - P_{23}B - P_{20}B, \frac{\partial}{\partial t} C = P_{23}B - P_{30}C \right]$$

$$\begin{bmatrix} \frac{\partial}{\partial t} A = P_{01} - \frac{BP_{12}A}{K} - P_{10}A \\ \frac{\partial}{\partial t} B = \frac{BP_{12}A}{K} - P_{23}B - P_{20}B \\ \frac{\partial}{\partial t} C = P_{23}B - P_{30}C \end{bmatrix}$$

```

> v:=M; alpha:='alpha': K:=k0; tA:=[1,15,35,50,58,62,73,nops(T)+dd]; kA:=['k1x||i' $ i=1..nops(tA)]
;

par:=[d0,k0,op(kA),k2a,k2b,k3];

param:=[
  P[`01`] = 0, P[`12`] = alpha(t,op(kA)), P[`23`] = beta(t,k2a,k2b),
  P[`10`] = 0, P[`20`] = k3
];

init:=[ A(-d0)=K, B(-d0)=1, C(-d0)=0 ];

```

$$\begin{aligned}
v &:= [A, B, C] \\
K &:= k0 \\
tA &:= [1, 15, 35, 50, 58, 62, 73, 80] \\
kA &:= [k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8] \\
par &:= [d0, k0, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8, k2a, k2b, k3] \\
param &:= [P_{01} = 0, P_{12} = \alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8), P_{23} = \beta(t, k2a, k2b), P_{10} = 0, P_{20} = k3] \\
init &:= [A(-d0) = k0, B(-d0) = 1, C(-d0) = 0]
\end{aligned}$$

(7)

```

> res:=solve(map(rhs,eqs[1..2]),v[1..2]); res:=res[2]: subs(P[`30`]=P[`10`],param,res);

J:=Matrix(subs(res,map(q->grad(rhs(q),v[1..2]),eqs[1..2]))); evalm(%-lambda): collect(Determinant
(%),lambda);

subs(P[`30`]=P[`10`],pr(param),%); solve(%,{lambda});

```

$$\begin{aligned}
res &:= \left[\left[A = \frac{P_{01}}{P_{10}}, B = 0 \right], \left[A = \frac{k0(P_{23} + P_{20})}{P_{12}}, B = -\frac{k0P_{10}P_{20} + k0P_{10}P_{23} - P_{01}P_{12}}{P_{12}(P_{23} + P_{20})} \right] \right] \\
&\quad \left[A = \frac{k0(\beta(t, k2a, k2b) + k3)}{\alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8)}, B = 0 \right]
\end{aligned}$$

$$J := \begin{bmatrix} \frac{k0 P_{10} P_{20} + k0 P_{10} P_{23} - P_{01} P_{12}}{(P_{23} + P_{20}) k0} & -P_{10} & -P_{23} & -P_{20} \\ -\frac{k0 P_{10} P_{20} + k0 P_{10} P_{23} - P_{01} P_{12}}{(P_{23} + P_{20}) k0} & & & 0 \end{bmatrix}$$

$$\frac{(k0 P_{20} + k0 P_{23}) \lambda^2}{(P_{23} + P_{20}) k0} + \frac{P_{01} P_{12} \lambda}{(P_{23} + P_{20}) k0} + \frac{-k0 P_{10} P_{20}^2 - 2 k0 P_{10} P_{20} P_{23} - k0 P_{10} P_{23}^2 + P_{01} P_{12} P_{20} + P_{01} P_{12} P_{23}}{(P_{23} + P_{20}) k0}$$

$$[P_{01} = 0, P_{12} = \alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8), P_{23} = \beta(t, k2a, k2b), P_{10} = 0, P_{20} = k3]$$

$$\frac{(k0 k3 + k0 \beta(t, k2a, k2b)) \lambda^2}{(\beta(t, k2a, k2b) + k3) k0}$$

$$\{\lambda = 0\}, \{\lambda = 0\}$$

(8)

```
> Eqs:=subs(map(q->q=q(t),v),Diff=diff,P[`30`]=P[`10`],param,eqs); #dsolve(%);
```

$$Eqs := \left[\frac{d}{dt} A(t) = -\frac{B(t) \alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8) A(t)}{k0}, \frac{d}{dt} B(t) \right]$$

(9)

$$= \frac{B(t) \alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8) A(t)}{k0} - \beta(t, k2a, k2b) B(t) - k3 B(t), \frac{d}{dt} C(t) = \beta(t, k2a, k2b) B(t)$$

```
> N:='N': A:='A': B:='B': C:='C': val:=valp:
```

```
#alpha:=unapply(simplify(evalf(piecewise(t<tA[1],kA[1],t<tA[2],Lag(t,tA[1..3],kA[1..3]),
# seq(op([t<tA[i+1],(Lag(t,tA[i-1..i+1],kA[i-1..i+1])+Lag(t,tA[i..i+2],kA[i..i+2]))/2]),i=2..nops
(kA)-2),
#t<tA[nops(tA)],Lag(t,tA[nops(tA)-2..nops(tA)],kA[nops(kA)-2..nops(kA)]),
#kA[nops(kA)]))) , t, op(kA));
```

```
alpha:=unapply(simplify(evalf(piecewise(t<tA[1],kA[1],t<tA[3],Lag(t,tA[1..4],kA[1..4]),
seq(op([t<tA[i+1],Lag(t,tA[i-1..i+2],kA[i-1..i+2])]),i=3..nops(kA)-3),
t<tA[nops(tA)],Lag(t,tA[nops(tA)-3..nops(tA)],kA[nops(kA)-3..nops(kA)]),
kA[nops(kA)]))) , t, op(kA));
```

```
beta:=(t,k2a,k2b)->piecewise(t<70,k2a,k2b);
```

```

EQS:=[op(Eqs),op(init)]:

res:=dsolve(EQS,numeric,map(q->q(t),v),output=listprocedure,parameters=par); assign('v[i]=subs
(res,v[i](t))' $ i=1..nops(v)):

chi2a:='chi2a': chi2:=unapply(chi2a(x0,xx,kA,x2a,x2b,x3),x0,xx,op(kA),x2a,x2b,x3):

chi2a:=proc(x0,xx,x1,x2a,x2b,x3) local i; global K; K:=xx;
  res(parameters=[corr(par,[x0,xx,op(x1),x2a,x2b,x3])]):
  sum((T[i]-K-A(i+dd))^2/(K-A(i+dd)),i=1..nops(T))+
  sum((T2[i]-B(i+dd))^2/B(i+dd),i=1..nops(T2))+
  sum((T1[i]-C(i+dd))^2/C(i+dd),i=1..nops(T1));
end:

chi2(op(pr(val))); val:=findMin(chi2,val); chi2(op(%));

#plot(map(q->q(t),v),t=0..3.0e4,legend=['`',```,``'],
#linestyle=[solid,dash,dashdot],gridlines=true);

writedata(cat(Region,`3c.txt`),val);

display(
  plot(map(q->q(t),v),t=0..300,legend=['`',```,``'],
  linestyle=[solid,dash,dashdot],gridlines=true),
  plot([[seq([i+dd,K-T[i]],i=1..nops(T))]],style=point,symbolsize=7,symbol=asterisk),
  plot([[seq([i+dd,T1[i]],i=1..nops(T1))]],style=point,symbolsize=7,symbol=circle),
  plot([[seq([i+dd,T2[i]],i=1..nops(T2))]],style=point,symbolsize=7,symbol=diamond,color=black),
  size=[1000,400],legendstyle=[font=[roman,15]]
): fdisplay(cat(Region,`3c`),%);

```

$$\alpha := (t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8) \mapsto \left\{ \begin{array}{l} (-0.00004287429258 \cdot k1x1 + 0.0001020408163 \cdot k1x2 - 0.00009803921574 \cdot k1x3 + 0.00000000000000 \cdot k1x4 \\ (-0.00003322259134 \cdot k1x2 + 0.0001449275363 \cdot k1x3 - 0.0002380952381 \cdot k1x4 + 0.00000000000000 \cdot k1x5 \\ (-0.0001073537306 \cdot k1x3 + 0.00069444444445 \cdot k1x4 - 0.00135869565217 \cdot k1x5 + 0.00000000000000 \cdot k1x6 \\ (-0.0004528985509 \cdot k1x4 + 0.0020833333333 \cdot k1x5 - 0.001893939394 \cdot k1x6 + 0.00000000000000 \cdot k1x7 \\ (-0.0007575757577 \cdot k1x5 + 0.001262626263 \cdot k1x6 - 0.0008658008661 \cdot k1x7 + 0.00000000000000 \cdot k1x8 \end{array} \right.$$

$$\beta := (t, k2a, k2b) \mapsto \begin{cases} k2a & t < 70 \\ k2b & \text{otherwise} \end{cases}$$

`res := [t = proc(t) ... end proc, A(t) = proc(t) ... end proc, B(t) = proc(t) ... end proc, C(t) = proc(t) ... end proc]`
 [12.11547222, 40685.61891, 0.08860157496, 0.1194914102, 0.206504248, 0.1639018944, 0.08136304104, 0.09362917651, 0.1050655024,
 0.104521194, 0.004380244938, 0.01024923215, 0.00009329616206]

2015.68898675881

2015.68898675881

2015.29675137787

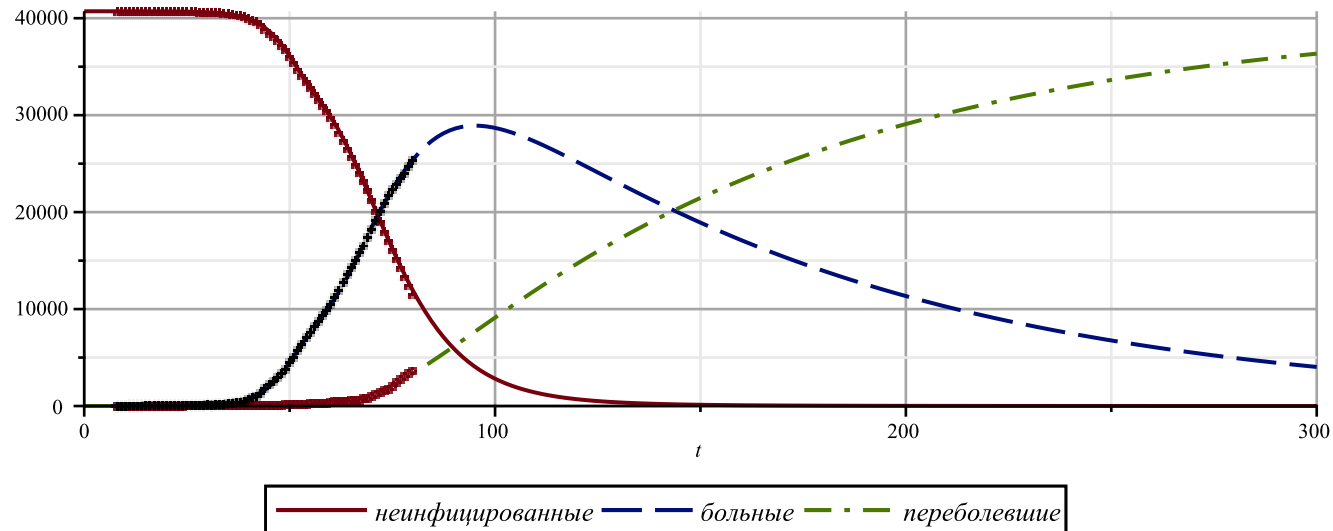
2015.01821812815

2013.77277387940
2012.82606401376
2012.55840325208
2012.20420344156
2012.08389553500

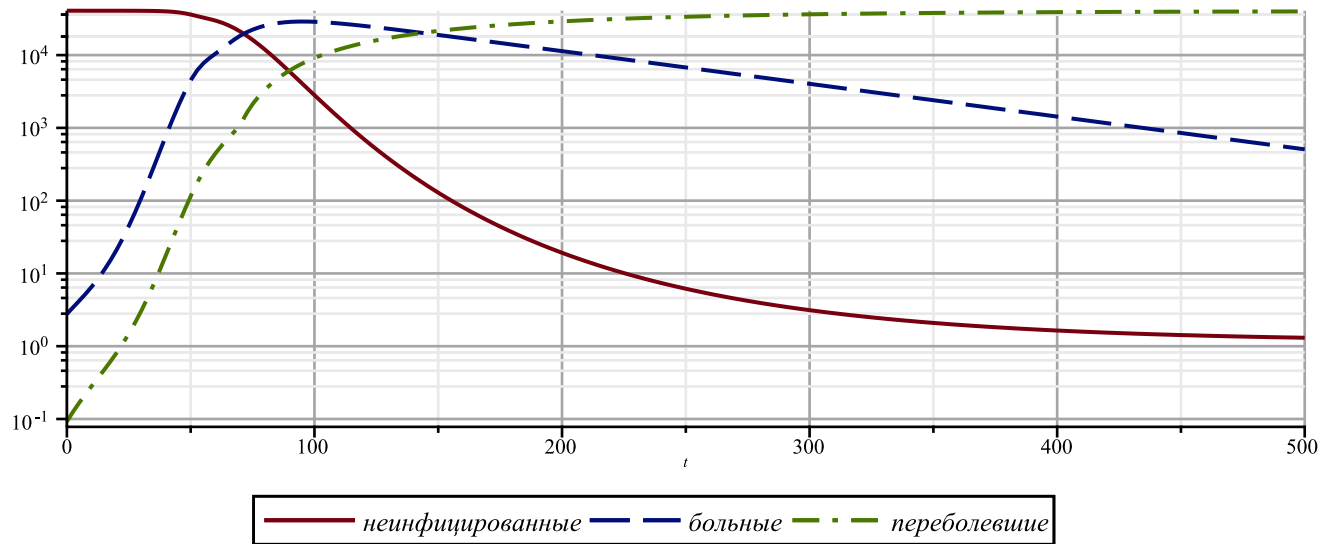
```
val := [12.1195611812185, 40717.7472873141, 0.0886366725340319, 0.119491590666531, 0.206380861976255, 0.163915548842873,  
0.0814150138728160, 0.0936182854924602, 0.105100345581347, 0.104541654636340, 0.00437603224366961, 0.0102735794662165,  
0.0000932963823698869]
```

2012.08389553500

Mosobl3c.jpg



```
> logplot(map(q->q(t),v), t=0..500, legend=[` ` , ` ` , ` ` ],  
linestyle=[solid,dash,dashdot],gridlines=true,size=[1000,400],legendstyle=[font=[roman,15]]);
```

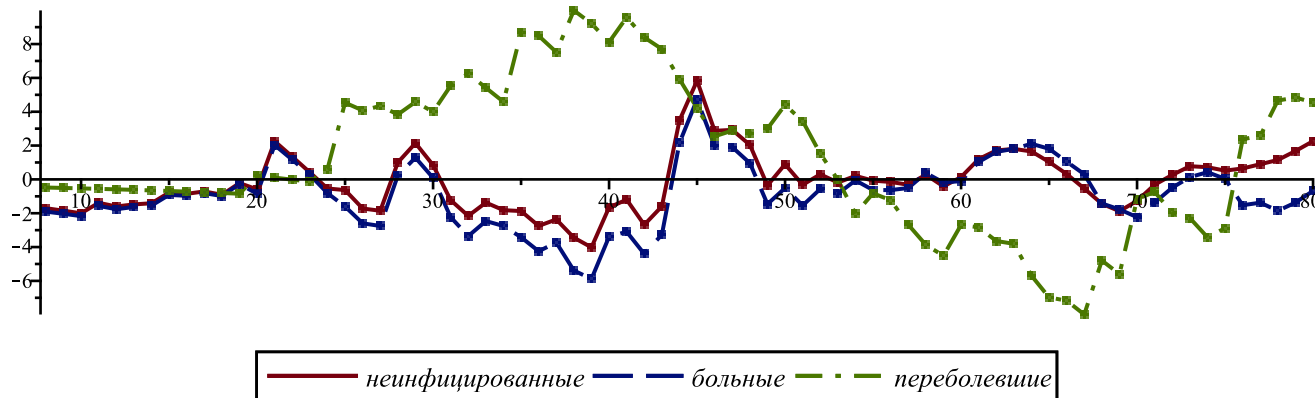


```

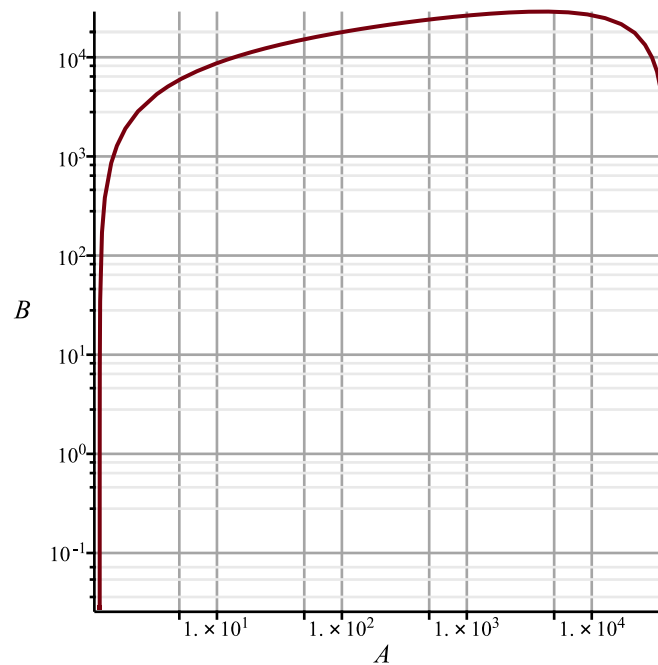
> display(
  plot([
    [[i, (T[i-dd]-(K -A(i)))/sigma(K -A(i))] $ i=1+dd..dd+nops(T)],
    [[i, (T2[i-dd]-(\bar{B}(i)))/sigma(B(i))) $ i=1+dd..dd+nops(T)],
    [[i, (T1[i-dd]-(C(i)))/sigma(C(i))] $ i=1+dd..dd+nops(T)]
  ], linestyle=[solid,dash,dashdot], legend = [ '\`', '\`', '\`' ]
  plot([
    [[i, (T[i-dd]-(K -A(i)))/sigma(K -A(i))] $ i=1+dd..dd+nops(T)],
    [[i, (T2[i-dd]-(\bar{B}(i)))/sigma(B(i))) $ i=1+dd..dd+nops(T)],
    [[i, (T1[i-dd]-(C(i)))/sigma(C(i))] $ i=1+dd..dd+nops(T)]
  ], style=point, symbolsize=8, symbol=solidcircle),
  size=[1000,300], legendstyle=[font=[roman,15]]
): fdisplay(cat(Region, `3c-dev`), %);

```

[Mosobl3c-dev.jpg](#)



```
> plot([v[1](t),v[2](t),t=0..3.0e4],axis[1]=[mode=log],axis[2]=[mode=log],labels=[v[1],v[2]],
labelfont=[roman,15],gridlines=true);
```



```
> [seq([i,(
(T[i-dd]-T[i-dd-1]) / (T2[i-dd]+T2[i-dd-1]) / ((1-T[i-dd]/K_)+(1-T[i-dd-1]/K_))
)*4],i=1+dd+1..nops(T)+dd)]: [seq([%[i][1],(%[i-1][2]+[%i][2]+[%i+1][2])/3],i=2..nops(%)-1)]:
```



```

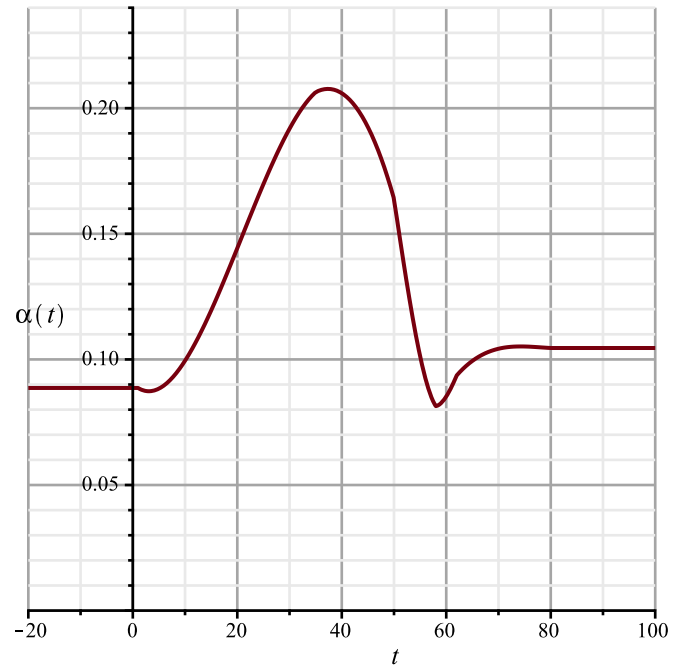
Palpha:=display(plot([%],color=blue),plot([%],style=point,symbolsize=8,symbol=solidcircle,color=
blue)):
#display(% ,gridlines=true,labels=['t','alpha(t)'],labelfont=[roman,15],view=[0..nops(T)+dd,0.
.0.9]);

subs(corr(par,val),alpha(t,op(kA)));
plot(% ,t=-20..100,gridlines=true,labels=['t','alpha(t)'],labelfont=[roman,15],view=[-20..100,0.
.0.24]):
fdisplay(cat(Region,'3c-zar'),%); display([Palpha,%],t i t l e = ' ' ,titlefont=
[roman,20]);

```

$$\left\{ \begin{array}{ll}
0.0886366725340319 & t < 1. \\
-5.46879439649574 \cdot 10^{-6} t^3 + 0.000341865597004780 t^2 - 0.00194794736543257 t + 0.0902482230147406 & t < 35. \\
-2.79699457536031 \cdot 10^{-6} t^3 + 0.0000746856183857201 t^2 + 0.00613424696842957 t + 0.0201134787797421 & t < 50. \\
0.0000532925928387916 t^3 - 0.00794612539426922 t^2 + 0.380812691354265 t - 5.67297964634473 & t < 58. \\
-0.0000542354355055108 t^3 + 0.0103336394228231 t^2 - 0.651026268667451 t + 13.6605598439999 & t < 62. \\
3.24433453390647 \cdot 10^{-6} t^3 - 0.000759956177024291 t^2 + 0.0591937691574649 t - 1.42833960705123 & t < 80. \\
0.104541654636340 & 80. \leq t
\end{array} \right.$$

Mosobl3c-zar.jpg



Коэффициент заражения

